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TECHNOLOGY**
**ON FIFTH MULTIPLICATIVE ZAGREB INDICES OF TETRATHIAFULVALENE
AND POPAM DENDRIMERS**

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ABSTRACT

A topological index is a numerical parameter mathematically derived from the graph structure. In this paper, we compute the general fifth multiplicative M-Zagreb indices, fifth multiplicative product connectivity index, fifth multiplicative sum connectivity index, fourth multiplicative atom bond connectivity index and fifth multiplicative geometric-arithmetic index of different chemically interesting dendrimers like tetrathiafulvalene and POPAM dendrimers.

Keywords: molecular graph, fifth multiplicative indices, connectivity indices, dendrimer.

Mathematics Subject Classification: 05C05, 05C07, 05C35.

I. INTRODUCTION

Let G be a finite, simple connected graph with vertex set $V(G)$ and edge set $E(G)$. A molecular graph is a simple graph related to the structure of a chemical compound. Each vertex of a molecular graph represents an atom of the molecule and its edges to the bonds between atoms. Let $S_G(u)$ denote the sum of the degrees of all vertices adjacent to a vertex u . For other undefined notations, readers may refer to [1].

Chemical Graph Theory has an important effect on the development of Chemical Sciences. A topological index is a numerical parameter mathematically derived from the graph structure. Numerous topological indices have been considered in Theoretical Chemistry, especially in quantitative structure activity (*QSAR*) and quantitative structure property (*QSPR*) study, see [2].

The fifth multiplicative Zagreb indices were introduced by Kulli in [3] and they are defined as

$$M_1G_5II(G) = \prod_{uv \in E(G)} [S_G(u) + S_G(v)], \quad M_2G_5II(G) = \prod_{uv \in E(G)} S_G(u)S_G(v).$$

In [4], Kulli introduced the fifth multiplicative hyper-Zagreb indices, the general fifth multiplicative Zagreb indices, fifth multiplicative product connectivity index, fifth multiplicative sum connectivity index. They are defined as follows:

The fifth multiplicative hyper-Zagreb indices of a graph G are defined as

$$HM_1G_5II(G) = \prod_{uv \in E(G)} [S_G(u) + S_G(v)]^2, \quad HM_2G_5II(G) = \prod_{uv \in E(G)} [S_G(u)S_G(v)]^2.$$

The fifth multiplicative sum connectivity index of a graph G is defined as

$$S_5II(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{S_G(u) + S_G(v)}}.$$

The fifth multiplicative product connectivity index of a graph G is defined as

$$P_5H(G) = \prod_{uv \in E(G)} \frac{1}{\sqrt{S_G(u)S_G(v)}}.$$

The general fifth multiplicative Zagreb indices of a graph G are defined as

$$M_1^a G_5H(G) = \prod_{uv \in E(G)} [S_G(u) + S_G(v)]^a,$$

$$M_2^a G_5H(G) = \prod_{uv \in E(G)} [S_G(u)S_G(v)]^a \quad (1)$$

where a is a real number.

In [5], Kulli introduced the fourth multiplicative atom bond connectivity index of a graph G and it is defined as

$$ABC_4H(G) = \prod_{uv \in E(G)} \sqrt{\frac{S_G(u) + S_G(v) - 2}{S_G(u)S_G(v)}}. \quad (2)$$

The fifth multiplicative geometric-arithmetic index of a graph G was introduced by Kulli in [3] and it is defined as

$$GA_5H(G) = \prod_{uv \in E(G)} \frac{2\sqrt{S_G(u)S_G(v)}}{S_G(u) + S_G(v)}. \quad (3)$$

Recently many other multiplicative indices were studied, for example, in [6, 7, 8, 9, 11, 12, 13, 14, 15, 16, 17, 18, 19].

In this paper, we compute the general fifth multiplicative M-Zagreb indices, fifth multiplicative product connectivity index, fifth multiplicative sum connectivity index, fourth multiplicative atom bond connectivity index and fifth multiplicative geometric-arithmetic index of tetrathiafulvalene and POPAM dendrimers. For more information about these dendrimers, see [20, 21].

II. TETRATHIAFULVALENE DENDRIMERS $TD_2[n]$

In this section, we focus on the molecular graph of a tetrathiafulvalene dendrimer. This family of tetrathiafulvalene dendrimers is denoted by $TD_2[n]$, where n is the steps of growth in this type of dendrimers for $n \geq 0$. The molecular graph of $TD_2[2]$ is shown in Figure 1.

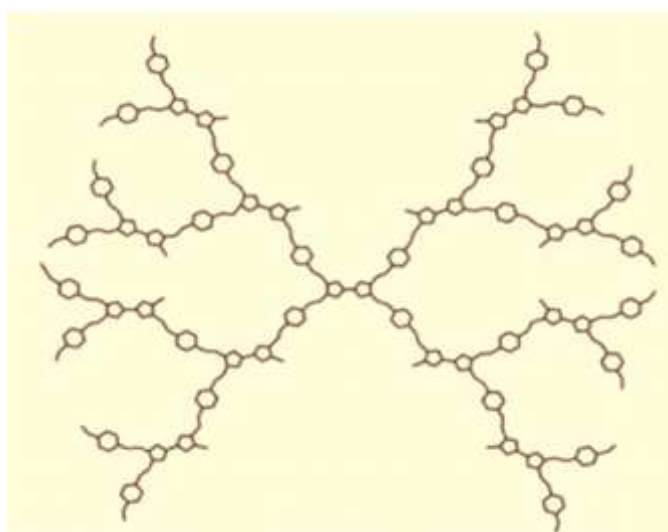


Figure 1. The molecular graph of $TD_2[2]$



Let G be the molecular graph of tetrathiafulvalene dendrimers $TD_2[n]$. By algebraic method, we obtain that $|V(G)|=31 \times 2^{n+2} - 74$ and $|E(G)|=35 \times 2^{n+2} - 85$. Also the edge partition of $TD_2[n]$ based on the degree sum of neighbors of end vertices of each edge is obtained as given in Table 1.

Table 1. Edge partition of $TD_2[n]$

| $S_G(u), S_G(v) uv \in E(G)$ | Number of edges |
|--------------------------------|--------------------------|
| (2, 4) | 2^{n+2} |
| (3, 6) | $2^{n+2} - 4$ |
| (4, 6) | 2^{n+2} |
| (5, 5) | $7 \times 2^{n+2} - 16$ |
| (5, 6) | $11 \times 2^{n+2} - 24$ |
| (5, 7) | $3 \times 2^{n+2} - 8$ |
| (6, 6) | $2^{n+2} - 4$ |
| (6, 7) | $8 \times 2^{n+2} - 24$ |
| (7, 7) | $2 \times 2^{n+2} - 5$ |

Theorem 1. The general fifth multiplicative M_1 -Zagreb index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$M_1^a G_5 II(G) = 6^{a(2^{n+2})} \times 9^{a(2^{n+2}-4)} \times 10^{a(8 \times 2^{n+2}-16)} \times 11^{a(11 \times 2^{n+2}-24)} \\ \times 12^{a(4 \times 2^{n+2}-12)} \times 13^{a(8 \times 2^{n+2}-24)} \times 14^{a(2 \times 2^{n+2}-5)}. \quad (4)$$

Proof: From equation (1) and Table 1, we derive

$$M_1^a G_5 II(G) = \prod_{uv \in E(G)} [S_G(u) + S_G(v)]^a \\ = 6^{a(2^{n+2})} \times 9^{a(2^{n+2}-4)} \times 10^{a(8 \times 2^{n+2}-16)} \times 11^{a(11 \times 2^{n+2}-24)} \\ \times 12^{a(4 \times 2^{n+2}-12)} \times 13^{a(8 \times 2^{n+2}-24)} \times 14^{a(2 \times 2^{n+2}-5)}.$$

Corollary 1.1. The fifth multiplicative M_1 -Zagreb index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$M_1 G_5 II(G) = 6^{2^{n+2}} \times 9^{2^{n+2}-4} \times 10^{8 \times 2^{n+2}-16} \times 11^{11 \times 2^{n+2}-24} \\ \times 12^{4 \times 2^{n+2}-12} \times 13^{8 \times 2^{n+2}-24} \times 14^{2 \times 2^{n+2}-5}.$$

Proof: Put $a = 1$ in equation (4), we get the desired result.

Corollary 1.2. The fifth multiplicative M_1 hyper-Zagreb index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$HM_1 G_5 II(G) = 6^{2^{n+3}} \times 9^{2^{n+3}-8} \times 10^{8 \times 2^{n+3}-32} \times 11^{11 \times 2^{n+3}-48} \\ \times 12^{4 \times 2^{n+3}-24} \times 13^{8 \times 2^{n+3}-48} \times 14^{2 \times 2^{n+3}-10}.$$

Proof: Put $a = 2$ in equation (4), we get the desired result.

Corollary 1.3. The fifth multiplicative sum connectivity index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$S_5 II(G) = \left(\frac{1}{\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{9}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{10}}\right)^{8 \times 2^{n+2}-16} \times \left(\frac{1}{\sqrt{11}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{\sqrt{12}}\right)^{4 \times 2^{n+2}-12} \times \left(\frac{1}{\sqrt{13}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{\sqrt{14}}\right)^{2 \times 2^{n+2}-5}.$$

Proof: Put $a = -\frac{1}{2}$ in equation (4), we get the desired result.

Theorem 2. The general fifth multiplicative M_2 -Zagreb index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$M_2^a G_5 II(G) = 8^{a \times 2^{n+2}} \times 18^{a(2^{n+2}-4)} \times 24^{a \times 2^{n+2}} \times 25^{a(7 \times 2^{n+2}-16)} \\ \times 30^{a(11 \times 2^{n+2}-24)} \times 35^{a(3 \times 2^{n+2}-8)} \times 36^{a(2^{n+2}-4)} \times 42^{a(8 \times 2^{n+2}-24)} \times 49^{a(2 \times 2^{n+2}-5)}. \quad (5)$$

Proof: From equation (1) and Table 1, we deduce

$$M_2^a G_5 II(G) = \prod_{uv \in E(G)} [S_G(u) S_G(v)]^a \\ = 8^{a \times 2^{n+2}} \times 18^{a(2^{n+2}-4)} \times 24^{a \times 2^{n+2}} \times 25^{a(7 \times 2^{n+2}-16)} \\ \times 30^{a(11 \times 2^{n+2}-24)} \times 35^{a(3 \times 2^{n+2}-8)} \times 36^{a(2^{n+2}-4)} \times 42^{a(8 \times 2^{n+2}-24)} \times 49^{a(2 \times 2^{n+2}-5)}.$$

Corollary 2.1. The fifth multiplicative M_2 -Zagreb index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$M_2 G_5 II(G) = 8^{2^{n+2}} \times 18^{2^{n+2}-4} \times 24^{2^{n+2}} \times 25^{7 \times 2^{n+2}-24} \\ \times 30^{11 \times 2^{n+2}-24} \times 35^{3 \times 2^{n+2}-8} \times 36^{2^{n+2}-4} \times 42^{8 \times 2^{n+2}-24} \times 49^{2 \times 2^{n+2}-5}.$$

Proof: Put $a = 1$ in equation (5), we get the desired result.

Corollary 2.2. The fifth multiplicative M_2 hyper-Zagreb index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$M_2 G_5 II(G) = 8^{2^{n+3}} \times 18^{2^{n+3}-8} \times 24^{2^{n+3}} \times 25^{7 \times 2^{n+3}-48} \\ \times 30^{11 \times 2^{n+3}-48} \times 35^{3 \times 2^{n+3}-16} \times 36^{2^{n+3}-8} \times 42^{8 \times 2^{n+3}-48} \times 49^{2 \times 2^{n+3}-10}.$$

Proof: Put $a = 2$ in equation (5), we get the desired result.

Corollary 2.3. The fifth multiplicative product connectivity index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$P_5 II(G) = \left(\frac{1}{\sqrt{8}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{18}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{24}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{25}}\right)^{7 \times 2^{n+2}-24} \times \left(\frac{1}{\sqrt{30}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{1}{\sqrt{35}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{1}{\sqrt{36}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{42}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{1}{\sqrt{49}}\right)^{2 \times 2^{n+2}-5}.$$

Proof: Put $a = -\frac{1}{2}$ in equation (5), we get the desired result.

Theorem 3. The fourth multiplicative atom bond connectivity index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$ABC_4 II(G) = \left(\frac{1}{\sqrt{2}}\right)^{2^{n+2}} \times \left(\frac{\sqrt{7}}{\sqrt{18}}\right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{3}}\right)^{2^{n+2}} \times \left(\frac{\sqrt{8}}{5}\right)^{7 \times 2^{n+2}-24} \times \left(\frac{\sqrt{3}}{\sqrt{10}}\right)^{11 \times 2^{n+2}-24} \\ \times \left(\frac{\sqrt{2}}{\sqrt{7}}\right)^{3 \times 2^{n+2}-8} \times \left(\frac{\sqrt{10}}{6}\right)^{2^{n+2}-4} \times \left(\frac{\sqrt{11}}{\sqrt{42}}\right)^{8 \times 2^{n+2}-24} \times \left(\frac{\sqrt{12}}{7}\right)^{2 \times 2^{n+2}-5}.$$

Proof: From equation (2) and Table 1, we derive

$$ABC_4 II(G) = \prod_{uv \in E(G)} \sqrt{\frac{S_G(u) + S_G(v) - 2}{S_G(u) S_G(v)}}$$

$$\begin{aligned}
&= \left(\sqrt{\frac{2+4-2}{2 \times 4}} \right)^{2^{n+2}} \times \left(\sqrt{\frac{3+6-2}{3 \times 6}} \right)^{2^{n+2}-4} \times \left(\sqrt{\frac{4+6-2}{4 \times 6}} \right)^{2^{n+2}} \times \left(\sqrt{\frac{5+5-2}{5 \times 5}} \right)^{7 \times 2^{n+2}-16} \times \left(\sqrt{\frac{5+6-2}{5 \times 6}} \right)^{11 \times 2^{n+2}-24} \\
&\times \left(\sqrt{\frac{5+7-2}{5 \times 7}} \right)^{3 \times 2^{n+2}-8} \times \left(\sqrt{\frac{6+6-2}{6 \times 6}} \right)^{2^{n+2}-4} \times \left(\sqrt{\frac{6+7-2}{6 \times 7}} \right)^{8 \times 2^{n+2}-24} \times \left(\sqrt{\frac{7+7-2}{7 \times 7}} \right)^{2 \times 2^{n+2}-5} \\
&= \left(\frac{1}{\sqrt{2}} \right)^{2^{n+2}} \times \left(\sqrt{\frac{7}{18}} \right)^{2^{n+2}-4} \times \left(\frac{1}{\sqrt{3}} \right)^{2^{n+2}} \times \left(\frac{\sqrt{8}}{5} \right)^{7 \times 2^{n+2}-16} \times \left(\sqrt{\frac{3}{10}} \right)^{11 \times 2^{n+2}-24} \\
&\times \left(\sqrt{\frac{2}{7}} \right)^{3 \times 2^{n+2}-8} \times \left(\frac{\sqrt{10}}{6} \right)^{2^{n+2}-4} \times \left(\sqrt{\frac{11}{42}} \right)^{8 \times 2^{n+2}-24} \times \left(\frac{\sqrt{12}}{7} \right)^{2 \times 2^{n+2}-5}
\end{aligned}$$

Theorem 4. The fifth multiplicative geometric-arithmetic index of a tetrathiafulvalene dendrimer $TD_2[n]$ is

$$GA_5 II(G) = \left(\frac{2\sqrt{2}}{3} \right)^{2(2^{n+2}-2)} \times \left(\frac{2\sqrt{6}}{5} \right)^{2^{n+2}} \times \left(\frac{2\sqrt{30}}{11} \right)^{11 \times 2^{n+2}-24} \times \left(\frac{\sqrt{35}}{6} \right)^{3 \times 2^{n+2}-8} \times \left(\frac{2\sqrt{42}}{13} \right)^{8 \times 2^{n+2}-24}$$

Proof: From equation (3) and Table 1, we derive

$$\begin{aligned}
GA_5 II(G) &= \prod_{uv \in E(G)} \frac{2\sqrt{S_G(u)S_G(v)}}{S_G(u) + S_G(v)} \\
&= \left(\frac{2\sqrt{2 \times 4}}{2+4} \right)^{2^{n+2}} \times \left(\frac{2\sqrt{3 \times 6}}{3+6} \right)^{2^{n+2}-4} \times \left(\frac{2\sqrt{4 \times 6}}{4+6} \right)^{2^{n+2}} \times \left(\frac{2\sqrt{5 \times 5}}{5+5} \right)^{7 \times 2^{n+2}-16} \times \left(\frac{2\sqrt{5 \times 6}}{5+6} \right)^{11 \times 2^{n+2}-24} \\
&\times \left(\frac{2\sqrt{5 \times 7}}{5+7} \right)^{3 \times 2^{n+2}-8} \times \left(\frac{2\sqrt{6 \times 6}}{6+6} \right)^{2^{n+2}-4} \times \left(\frac{2\sqrt{6 \times 7}}{6+7} \right)^{8 \times 2^{n+2}-24} \times \left(\frac{2\sqrt{7 \times 7}}{7+7} \right)^{2 \times 2^{n+2}-5} \\
&= \left(\frac{2\sqrt{2}}{3} \right)^{2(2^{n+2}-2)} \times \left(\frac{2\sqrt{6}}{5} \right)^{2^{n+2}} \times \left(\frac{2\sqrt{30}}{11} \right)^{11 \times 2^{n+2}-24} \times \left(\frac{\sqrt{35}}{6} \right)^{3 \times 2^{n+2}-8} \times \left(\frac{2\sqrt{42}}{13} \right)^{8 \times 2^{n+2}-24}
\end{aligned}$$

III. POPAM DENDRIMERS $TD_2[n]$

In this section, we focus on the molecular graph of POPAM dendrimers. This family of dendrimers is denoted by $POD_2[n]$, where n is the steps of growth in this type of dendrimers. The molecular graph of $POD_2[2]$ is shown in Figure 2.

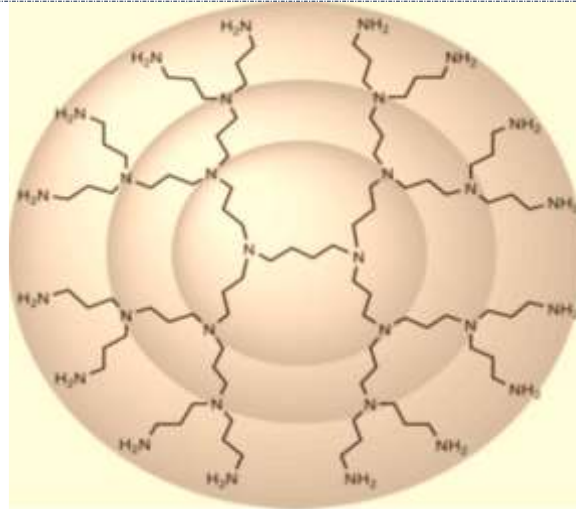


Figure 2. The graph of POPAM dendrimer $POD_2[2]$

Let G be the molecular graph of POPAM dendrimers $POD_2[n]$. By algebraic method, we obtain that $|V(POD_2[n])| = 2^{n+5} - 10$ and $|E(POD_2[n])| = 2^{n+5} - 11$. The edge partition of $POD_2[n]$ based on the degree sum of neighbors of end vertices of each edge is obtained as given in Table 2.

Table 2. Edge partition of $POD_2[n]$

| $S_G(u), S_G(v) uv \in E(G)$ | (2, 3) | (3, 4) | (4, 4) | (4, 5) | (5, 6) |
|--------------------------------|-----------|-----------|--------|--------------------|--------------------|
| Number of edges | 2^{n+2} | 2^{n+2} | 1 | $3 \times 2^n - 6$ | $3 \times 2^n - 6$ |

Theorem 5. The general fifth multiplicative M_1 -Zagreb index of a POPAM dendrimer $POD_2[n]$ is

$$M_1^a G_5 II(G) = 5^{a(2^{n+2})} \times 7^{a(2^{n+2})} \times 8^a \times 9^{a(3 \times 2^n - 6)} \times 11^{a(3 \times 2^n - 6)}. \tag{6}$$

Proof: From equation (1) and Table 2, we derive

$$\begin{aligned} M_1^a G_5 II(G) &= \prod_{uv \in E(G)} [S_G(u) + S_G(v)]^a \\ &= 5^{a(2^{n+2})} \times 7^{a(2^{n+2})} \times 8^a \times 9^{a(3 \times 2^n - 6)} \times 11^{a(3 \times 2^n - 6)}. \end{aligned}$$

Corollary 5.1. The fifth multiplicative M_1 -Zagreb index of a POPAM dendrimer $POD_2[n]$ is

$$M_1 G_5 II(G) = 5^{2^{n+2}} \times 7^{2^{n+2}} \times 8 \times 9^{3 \times 2^n - 6} \times 11^{3 \times 2^n - 6}.$$

Proof: Put $a = 1$ in equation (6), we get the desired result.

Corollary 5.2. The fifth multiplicative M_1 hyper-Zagreb index of a POPAM dendrimer $POD_2[n]$ is

$$HM_1 G_5 II(G) = 5^{2 \times 2^{n+2}} \times 7^{2 \times 2^{n+2}} \times 8^2 \times 9^{2(3 \times 2^n - 6)} \times 11^{2(3 \times 2^n - 6)}.$$

Proof: Put $a = 2$ in equation (6), we get the desired result.

Corollary 5.3. The fifth multiplicative sum connectivity index of a POPAM dendrimer $POD_2[n]$ is

$$S_5 II(G) = \left(\frac{1}{\sqrt{5}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{7}}\right)^{2^{n+2}} \times \left(\frac{1}{2\sqrt{2}}\right) \times \left(\frac{1}{3}\right)^{3 \times 2^n - 6} \times \left(\frac{1}{\sqrt{11}}\right)^{3 \times 2^n - 6}.$$

Proof: Put $a = -\frac{1}{2}$ in equation (6), we get the desired result.

Theorem 6. The general fifth multiplicative M_2 -Zagreb index of a POPAM dendrimer $POD_2[n]$ is

$$M_2^a G_5 II(G) = 6^{a \times 2^{n+2}} \times 12^{a \times 2^{n+2}} \times 16^a \times 20^{a(3 \times 2^n - 6)} \times 30^{a(3 \times 2^n - 6)}. \quad (7)$$

Proof: From equation (1) and Table 2, we derive

$$M_2^a G_5 II(G) = \prod_{uv \in E(G)} [S_G(u)S_G(v)]^a = 6^{a \times 2^{n+2}} \times 12^{a \times 2^{n+2}} \times 16^a \times 20^{a(3 \times 2^n - 6)} \times 30^{a(3 \times 2^n - 6)}.$$

Corollary 6.1. The fifth multiplicative M_2 -Zagreb index of a POPAM dendrimer $POD_2[n]$ is

$$M_2 G_5 II(G) = 6^{2^{n+2}} \times 12^{2^{n+2}} \times 16 \times 20^{3 \times 2^n - 6} \times 30^{3 \times 2^n - 6}$$

Proof: Put $a = 1$ in equation (7), we get the desired result.

Corollary 6.2. The fifth multiplicative M_2 hyper-Zagreb index of a POPAM dendrimer $POD_2[n]$ is

$$HM_2 G_5 II(G) = 6^{2^{n+3}} \times 12^{2^{n+3}} \times 16^2 \times 20^{2(3 \times 2^n - 6)} \times 30^{2(3 \times 2^n - 6)}.$$

Proof: Put $a = 2$ in equation (7), we get the desired result.

Corollary 6.3. The fifth multiplicative product connectivity index of a POPAM dendrimer $POD_2[n]$ is

$$P_5 II(G) = \left(\frac{1}{\sqrt{6}}\right)^{2^{n+2}} \times \left(\frac{1}{\sqrt{12}}\right)^{2^{n+2}} \times \left(\frac{1}{4}\right) \times \left(\frac{1}{\sqrt{20}}\right)^{3 \times 2^n - 6} \times \left(\frac{1}{\sqrt{30}}\right)^{3 \times 2^n - 6}.$$

Proof: Put $a = -\frac{1}{2}$ in equation (7), we get the desired result.

Theorem 7. The fourth multiplicative atom bond connectivity index of a POPAM dendrimer $POD_2[n]$ is

$$ABC_4 II(G) = \left(\frac{1}{\sqrt{2}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{5}{12}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{3}{8}}\right) \times \left(\sqrt{\frac{7}{20}}\right)^{3 \times 2^n - 6} \times \left(\sqrt{\frac{3}{10}}\right)^{3 \times 2^n - 6}.$$

Proof: From equation (2) and Table 2, we deduce

$$\begin{aligned} ABC_4 II(G) &= \prod_{uv \in E(G)} \sqrt{\frac{S_G(u) + S_G(v) - 2}{S_G(u)S_G(v)}} \\ &= \left(\sqrt{\frac{2+3-2}{2 \times 3}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{3+4-2}{3 \times 4}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{4+4-2}{4 \times 4}}\right)^1 \times \left(\sqrt{\frac{4+5-2}{4 \times 5}}\right)^{3 \times 2^n - 6} \times \left(\sqrt{\frac{5+6-2}{5 \times 6}}\right)^{3 \times 2^n - 6} \\ &= \left(\frac{1}{\sqrt{2}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{5}{12}}\right)^{2^{n+2}} \times \left(\sqrt{\frac{3}{8}}\right)^1 \times \left(\sqrt{\frac{7}{20}}\right)^{3 \times 2^n - 6} \times \left(\sqrt{\frac{3}{10}}\right)^{3 \times 2^n - 6}. \end{aligned}$$

Theorem 8. The fifth multiplicative geometric-arithmetical index of a POPAM dendrimer $POD_2[n]$ is

$$GA_5 II(G) = \left(\frac{2\sqrt{6}}{5}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{12}}{7}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{20}}{9}\right)^{3 \times 2^{n+2} - 6} \times \left(\frac{2\sqrt{30}}{11}\right)^{3 \times 2^n - 6}.$$

Proof: From equation (3) and Table 2, we deduce

$$\begin{aligned}
 GA_5II(G) &= \prod_{uv \in E(G)} \frac{2\sqrt{S_G(u)S_G(v)}}{S_G(u) + S_G(v)} \\
 &= \left(\frac{2\sqrt{2 \times 3}}{2+3}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{3 \times 4}}{3+4}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{4 \times 4}}{4+4}\right)^1 \times \left(\frac{2\sqrt{4 \times 5}}{4+5}\right)^{3 \times 2^n - 6} \times \left(\frac{2\sqrt{5 \times 6}}{5+6}\right)^{3 \times 2^n - 6} \\
 &= \left(\frac{2\sqrt{6}}{5}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{12}}{7}\right)^{2^{n+2}} \times \left(\frac{2\sqrt{20}}{9}\right)^{3 \times 2^n - 6} \times \left(\frac{2\sqrt{30}}{11}\right)^{3 \times 2^n - 6}.
 \end{aligned}$$

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